Lesson #4: More Distributive Property and Powers of Monomials

Learning Goal: We are learning to expand and simplify more complicated expressions.

Let's start off by continuing our lesson on the Distributive Property. Take a look at the following questions:

Expand AND simplify (put your answers in descending order):

a)
$$3x(4x^2-7x+2)+4x^2(2x-3)$$

b)
$$-4y^2(3y^2-5)-5y^3(6+y)$$

c)
$$3mn(2m-7n)-5m^2(4n+8)+6n^2(3m-n)$$

Now we are going to go back to discussing monomials. How do we simplify $(3x^2y^5)^3$? This is called a monomial raised to a power. How does the outside exponent affect the question? First, how does it work with just a number?

Simplify $\left(4^3\right)^2$

The initial exponents were 3 and 2, with the final exponent a _____. So, 3 _____ 2 = ____! This leads to our second exponent law. When raising a power to a power, ______ the exponents. Try it out!

a) $\left(\chi^4\right)^5$

b) $(y^2)^8$

c) $(m^3 n^6)^4$

That's all well and good (hopefully), but how do you handle a question with a coefficient?

Consider the expression from before, $(3x^2y^5)^3$. Expand it without using the laws.

The coefficient was just raised to the power of 3! Awesome. Try out some more, this time following the laws.

a)
$$(2x^4y^2)^5$$

b)
$$\left(-3m^7n\right)^2$$

c)
$$(5a^2b^3c^4d^5)^6$$

d)
$$(3x^2y^5)^2(2xy^3)$$

e)
$$(-4m^3n^2)^3(3m^4n^3)^2$$

f)
$$(5x^2y^4z^6)^0$$
 Whoah!! Exponent of zero? How does that work?

There are multiple explanations. We will look at a pattern, starting with 4^1 then moving up the ladder.

 $4^4 =$

 $4^{3} =$

 $4^2 =$

4 =

 $4^{1} =$

 $4^{0} =$

As you move up the ladder, you keep multiplying by 4. If you were to go down the ladder, you would ______ by 4. Follow the pattern to determine what four to the power of

zero is.

This leads to another exponent law: Anything to the power of

zero is equal to _____.

$$\left(5x^2y^4z^6\right)^0 =$$

Success Criteria:

- I can use the distributive property to multiply a polynomial with a monomial
- I can use the distributive property to combine multiple variables into a single term
- I can simplify a monomial raised to a power by multiplying the exponents of each variable
- I can recognize that when a coefficient is raised to a power, it is NOT NOT NOT multiplied
- I can understand that raising to the power of zero equals one.